

Refined turbulence modelling for reactor thermal-hydraulics

Part of UK's “**K**eeping **N**uclear **O**ptions **O**pen” project



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KNOO

Keeping the Nuclear Option Open

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Keeping the Nuclear Option Open
part of the Research Councils UK Energy Programm

<http://www.knoo.org/>

- to maintain and develop skills relevant to nuclear power generation.
- 4 years, 6M £, 50 PhDs and Post-docs,
- largest commitment to fission reactor research in UK for over 30 years,
- collaboration with industrial and governmental stakeholders and international partners.



Attendees at the KNOO annual meeting at HMS Sultan.

MANCHESTER
1824

University of
BRISTOL

CARDIFF
UNIVERSITY
PRIFYSGOL
CAERDYDD

Imperial College
London



The University
Of
Sheffield.

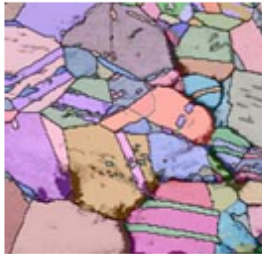
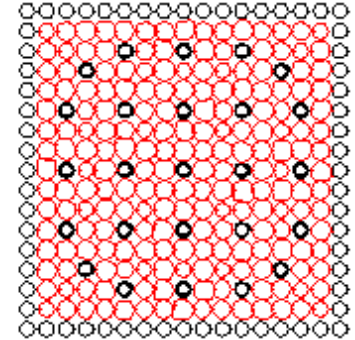


The Open University

Themes – Work Packages

W/P1. Fuel, thermal hydraulics and reactor systems

Coupling of multi-pin structural mechanics and three-dimensional transient two phase thermal hydraulic analysis for the study of severe accidents (e.g. pin ballooning under reflood conditions); crud deposition and its thermal hydraulic and neutronic effects; application of advanced CFD to Generation IV systems.



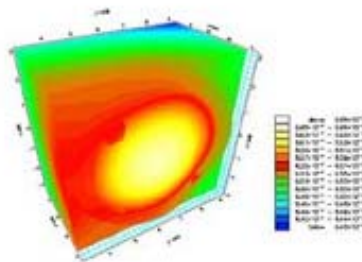
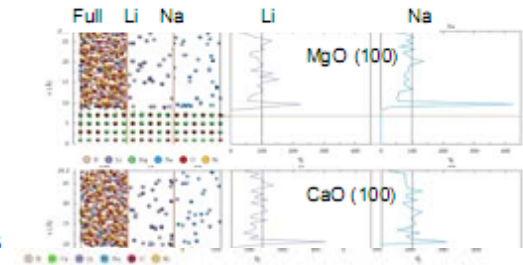
EBSD image of SCC
in stainless steel

W/P 2. Materials performance and monitoring reactor conditions

Remote structural interrogation and monitoring tools; miniaturised, encapsulated monitoring systems; FE/self consistent models to assess materials; mechanical understanding and predictive models of SCC; mechanical performance of nuclear cladding and structural materials; behaviour of graphite

W/P 3. An integrated approach to waste immobilization and management

Re-mobilisation, transport, solid-liquid separation, and immobilisation of particulate wastes; develop predictive models for particle behaviour based on atomic scale, thermodynamic and process scale simulations; develop fundamental understanding of selective adsorbing of nuclides onto filter systems

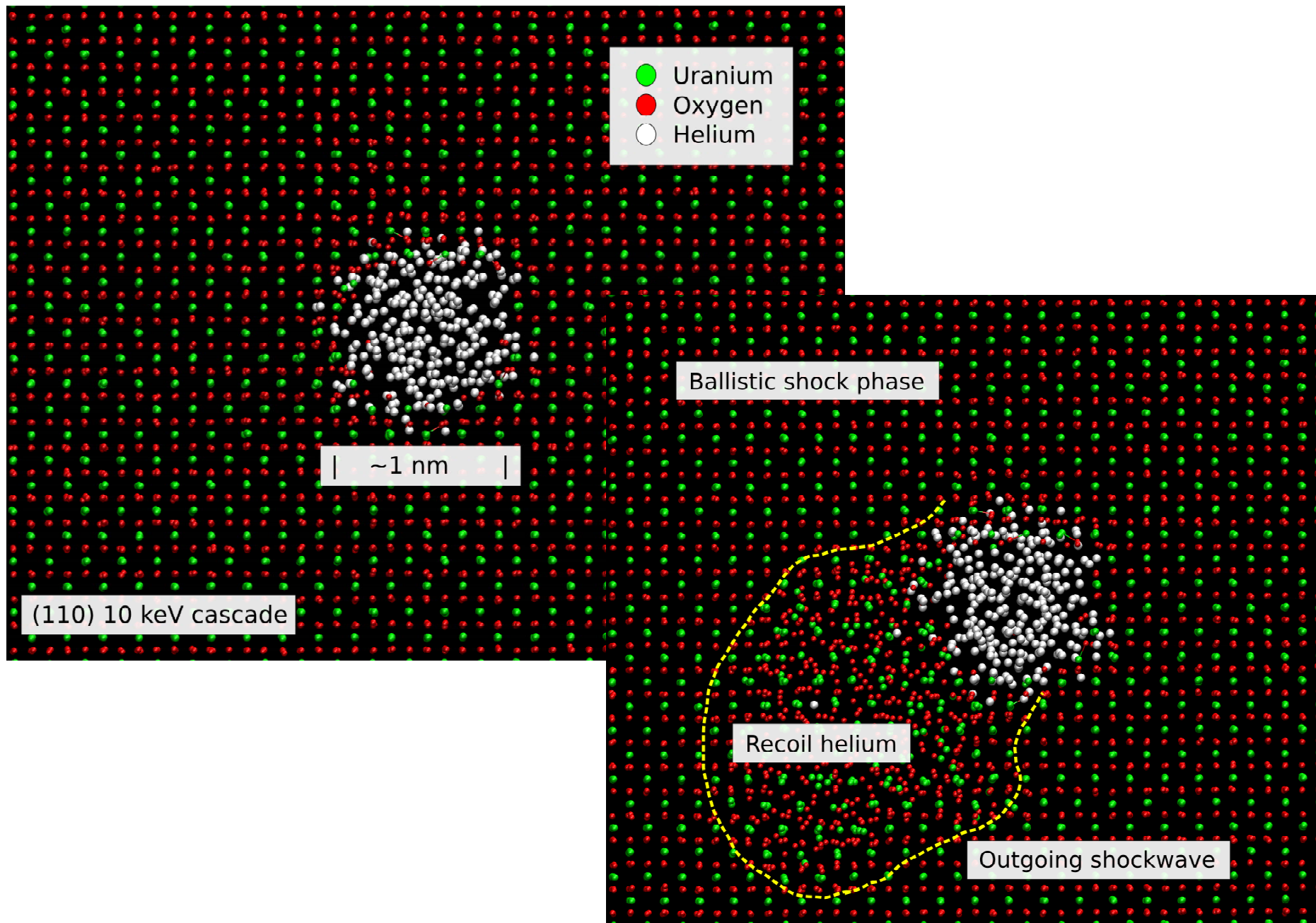


6.2 core sphere embedded in 6.2cm cuboid (quad mesh)

W/P 4. Safety and performance for a new generation of reactor designs

3D plant fault/severe accident transient studies that match UK industry plans for Generation IV (VHTR, GFR and SFR); assess demands on candidate materials under transient and normal operating conditions; scope safety approaches for the hydrogen production process and systems.

Ex: Molecular dynamics of radiation enhanced helium re-solution



Heat transfer through crud

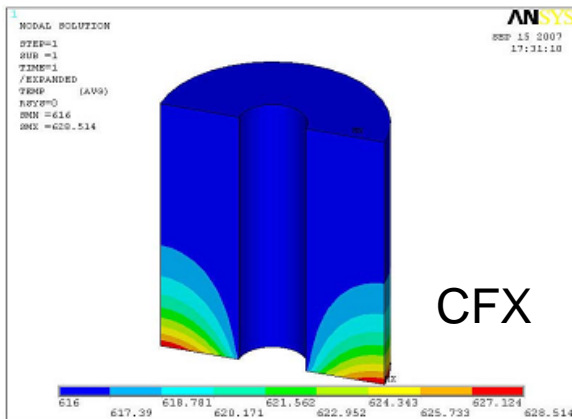


Fig. 1 Temperature contours in the porous shell of the crud

Droplets on hot solid surfaces: Modelling and Experimentation

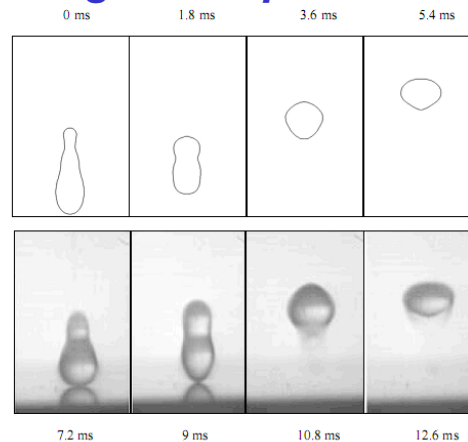
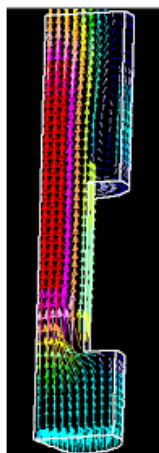


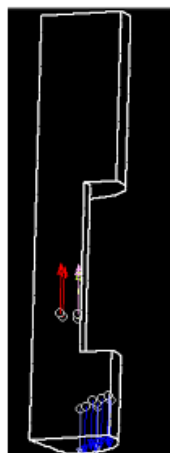
Fig. 1. Comparison between two-dimensional axisymmetric simulation of a millimetric droplet impacting on a 300°C solid surface ($We=11$) and experimental results by Bianco et al (2006) ($We=10$). The time interval between pictures is 1.8 ms.

Ballooning fuel pins

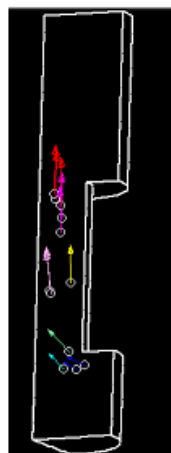
STAR



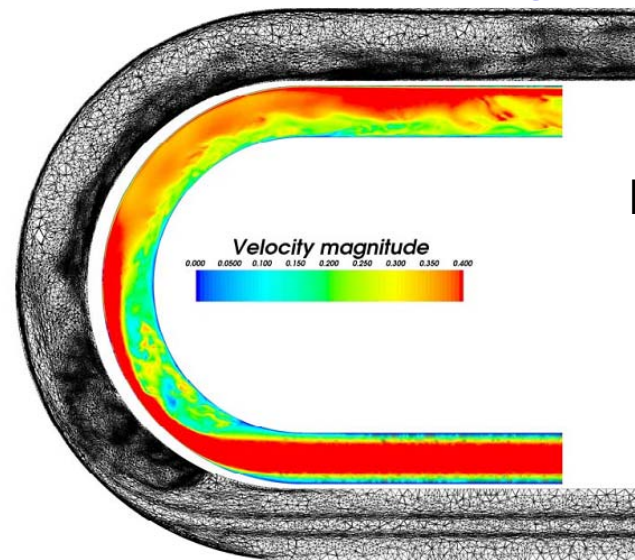
Vapour Flow Velocity Vectors



Droplets Path, (a) Particles of Water Density, (b) Particles of Smaller Density (1.2kg/m^3)



LES with adaptive FE meshing



FE (Fetch

Figure 1 Time snapshot (with a slice through the domain) of flow velocity and adapted mesh for LES modelling of flow through a circular cross section U bend pipe.

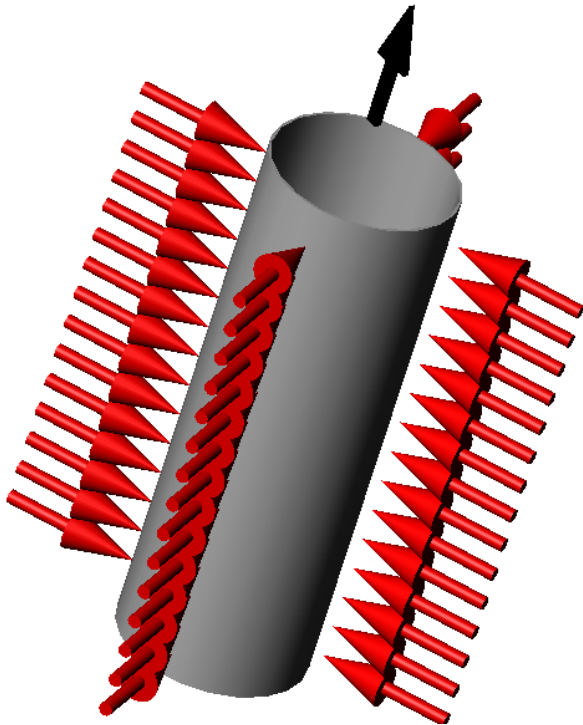
Test Case 1 : Mixed convection in vertically flowing heated pipe (buoyancy aiding or opposing)

Problem specifications:

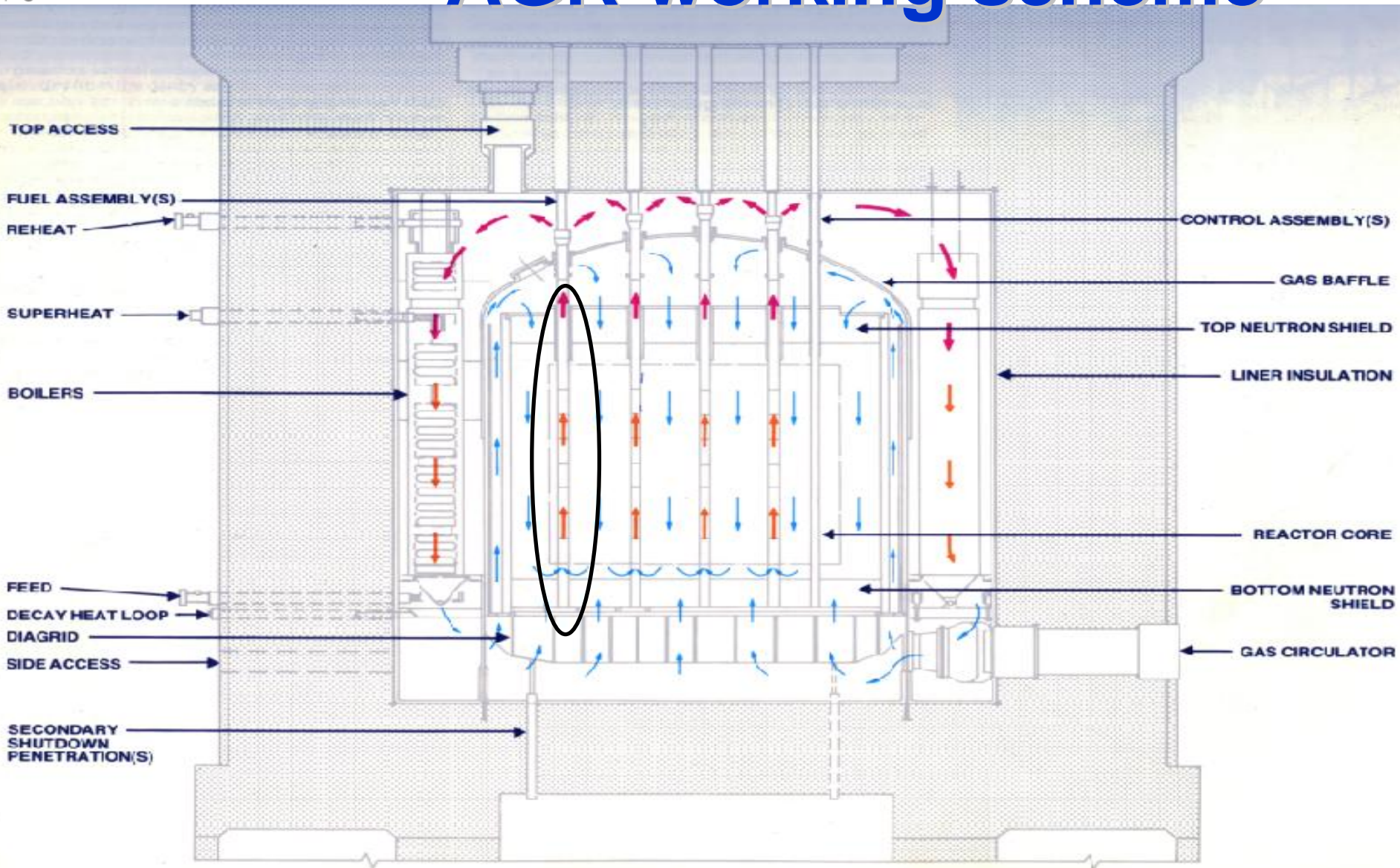
- $Re=2650$
- $Pr=0.71$
- Wall constant heat flux
- Boussinesq approximation

Heat transfer Regimes:

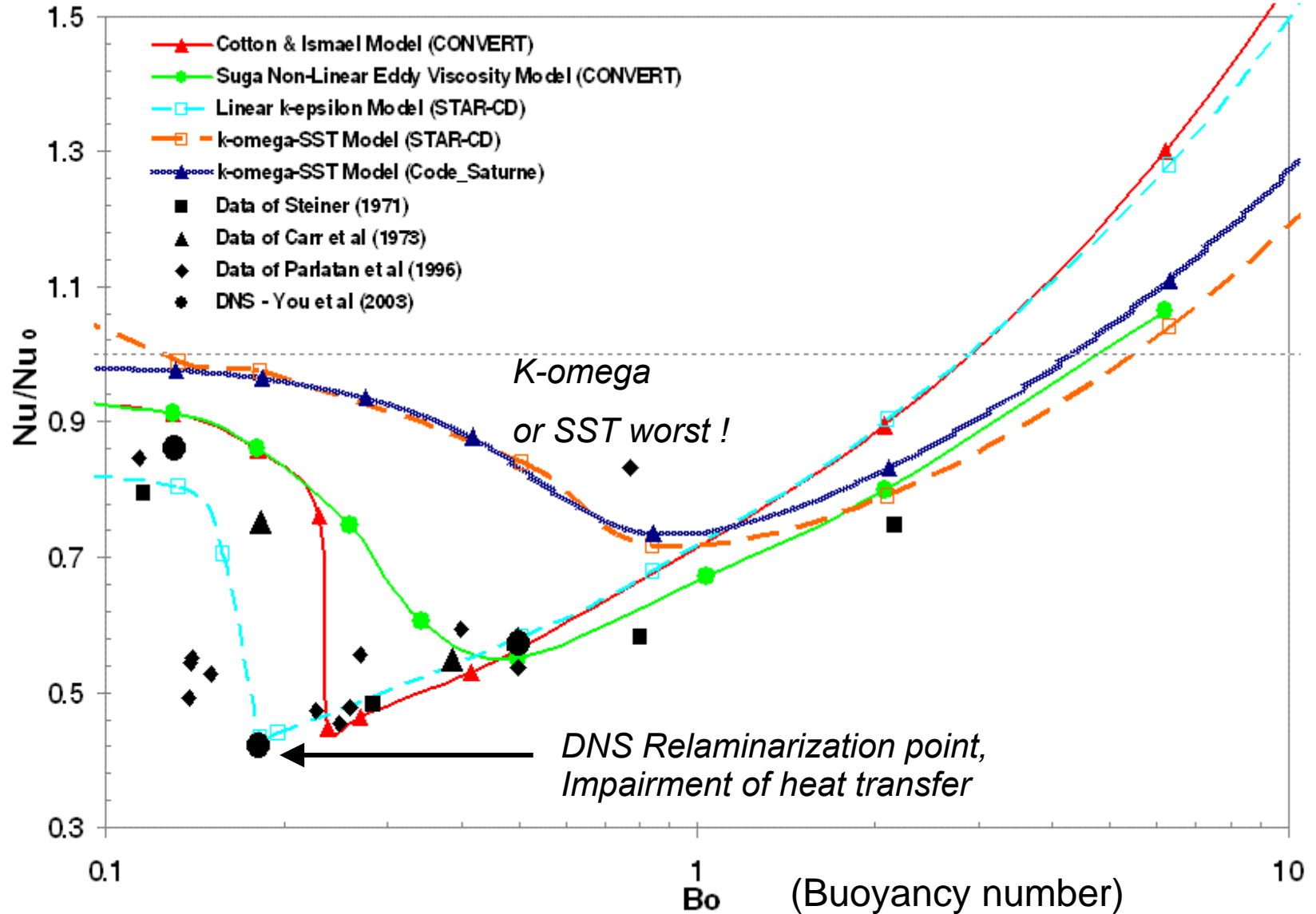
- $Gr/Re^2=0.000 \rightarrow$ Forced Convection
- $Gr/Re^2=0.063 \rightarrow$ Forced/Mixed Convection
- $Gr/Re^2=0.087 \rightarrow$ Re-Laminarization
- $Gr/Re^2=0.241 \rightarrow$ Recovery



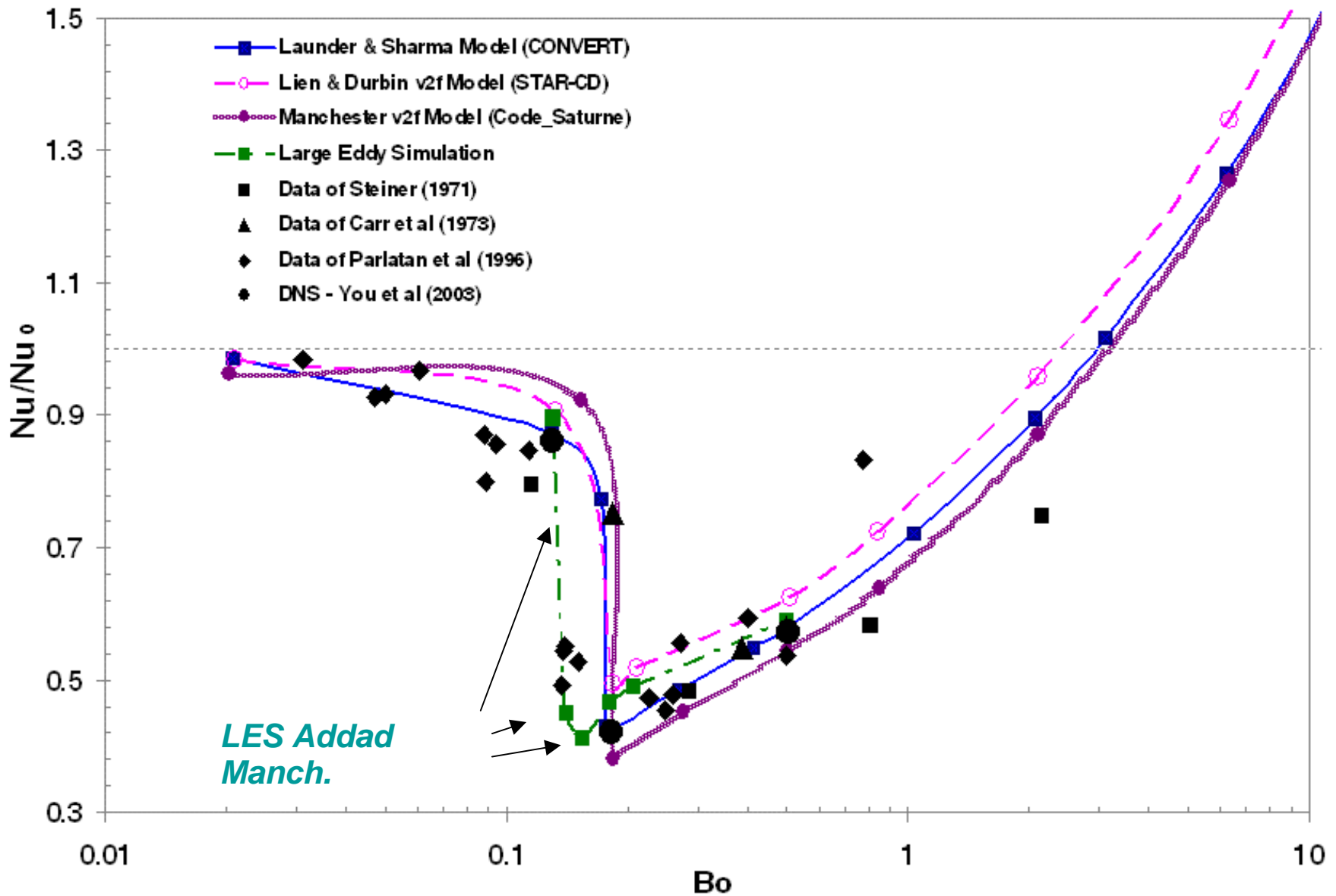
AGR working scheme



Range of RANS models



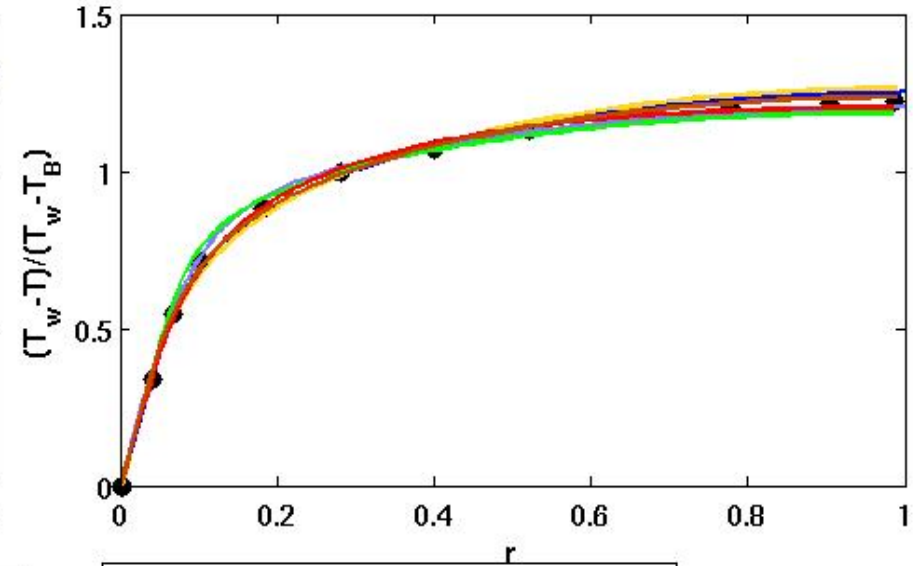
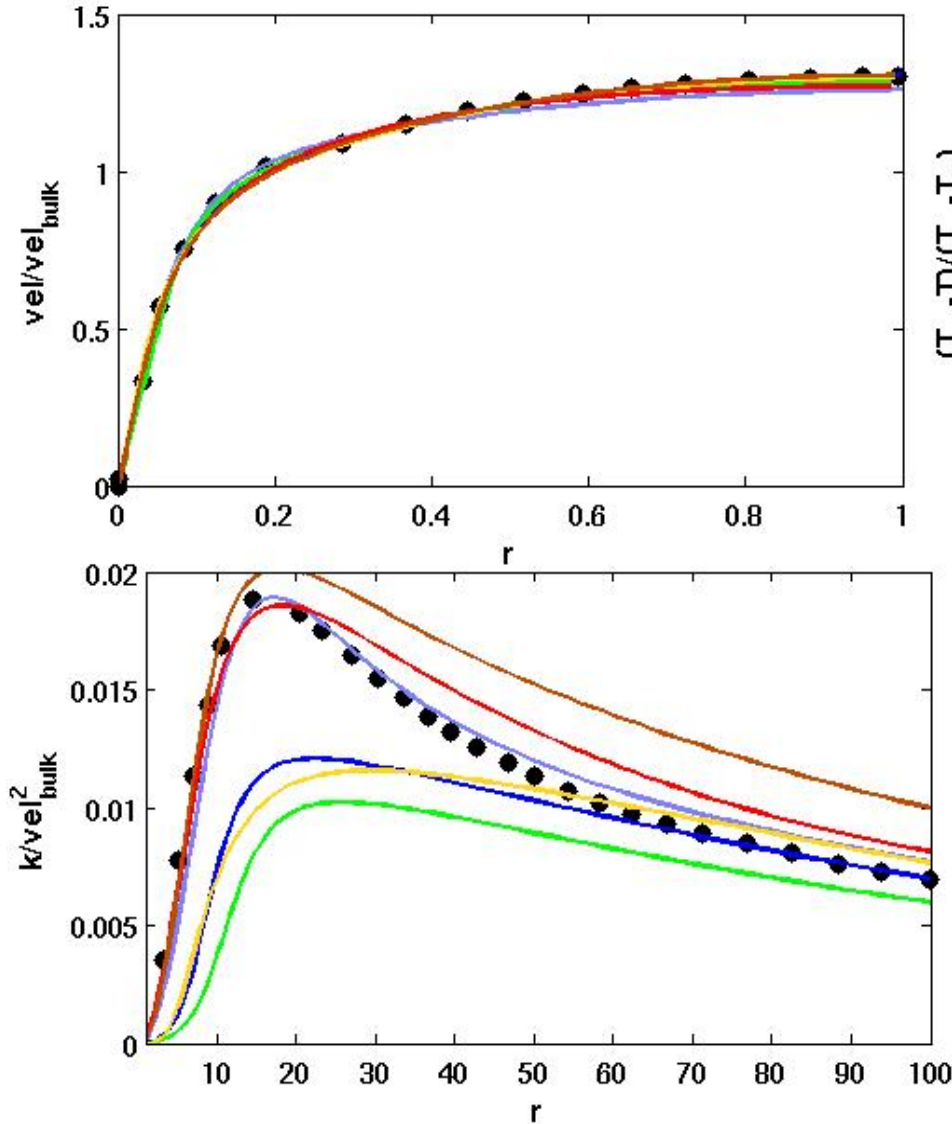
best models: Launder Sharma, V2F



Buoyancy aided heated pipe flow

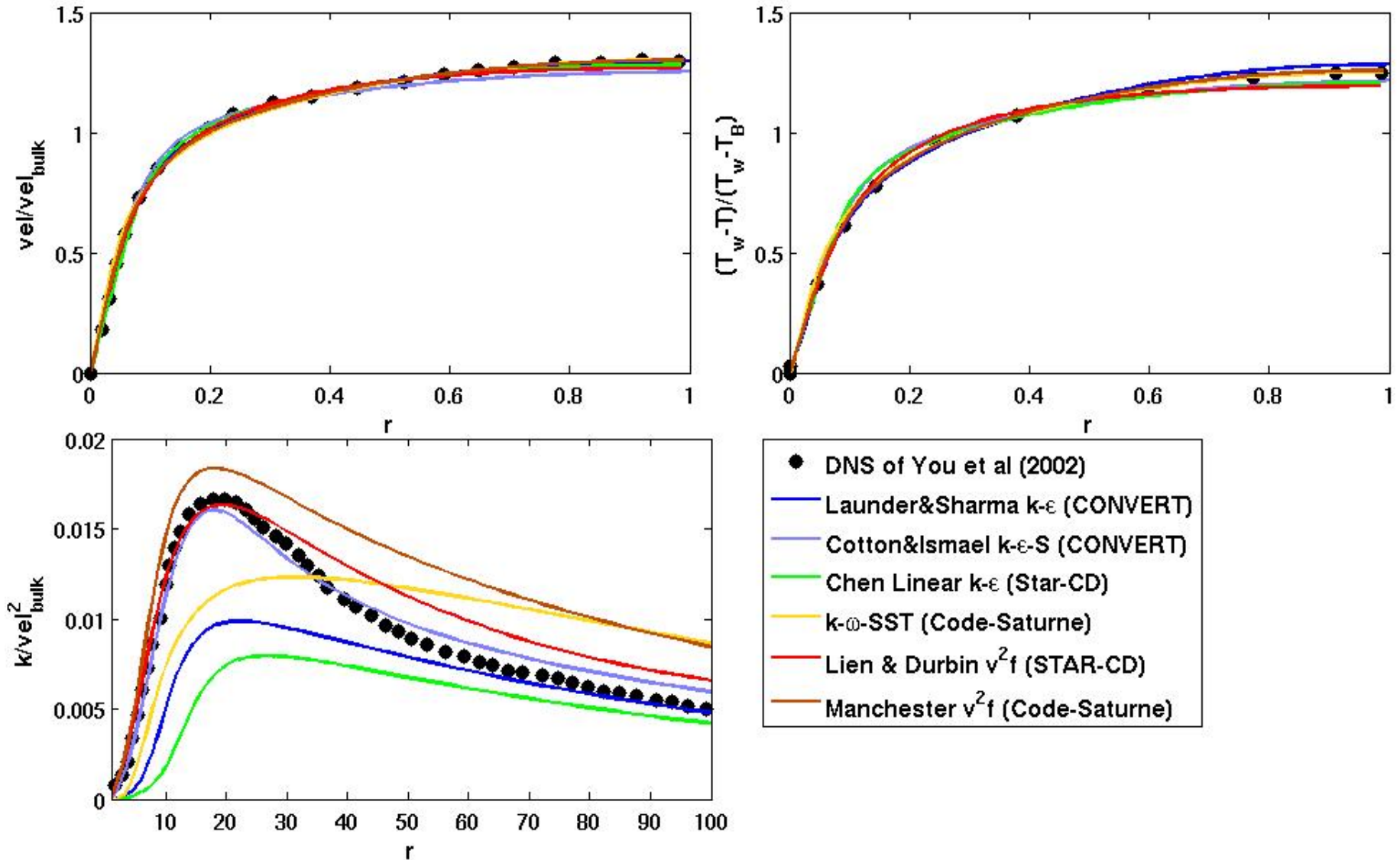


$$Gr/Re^{**2} = 0.000$$

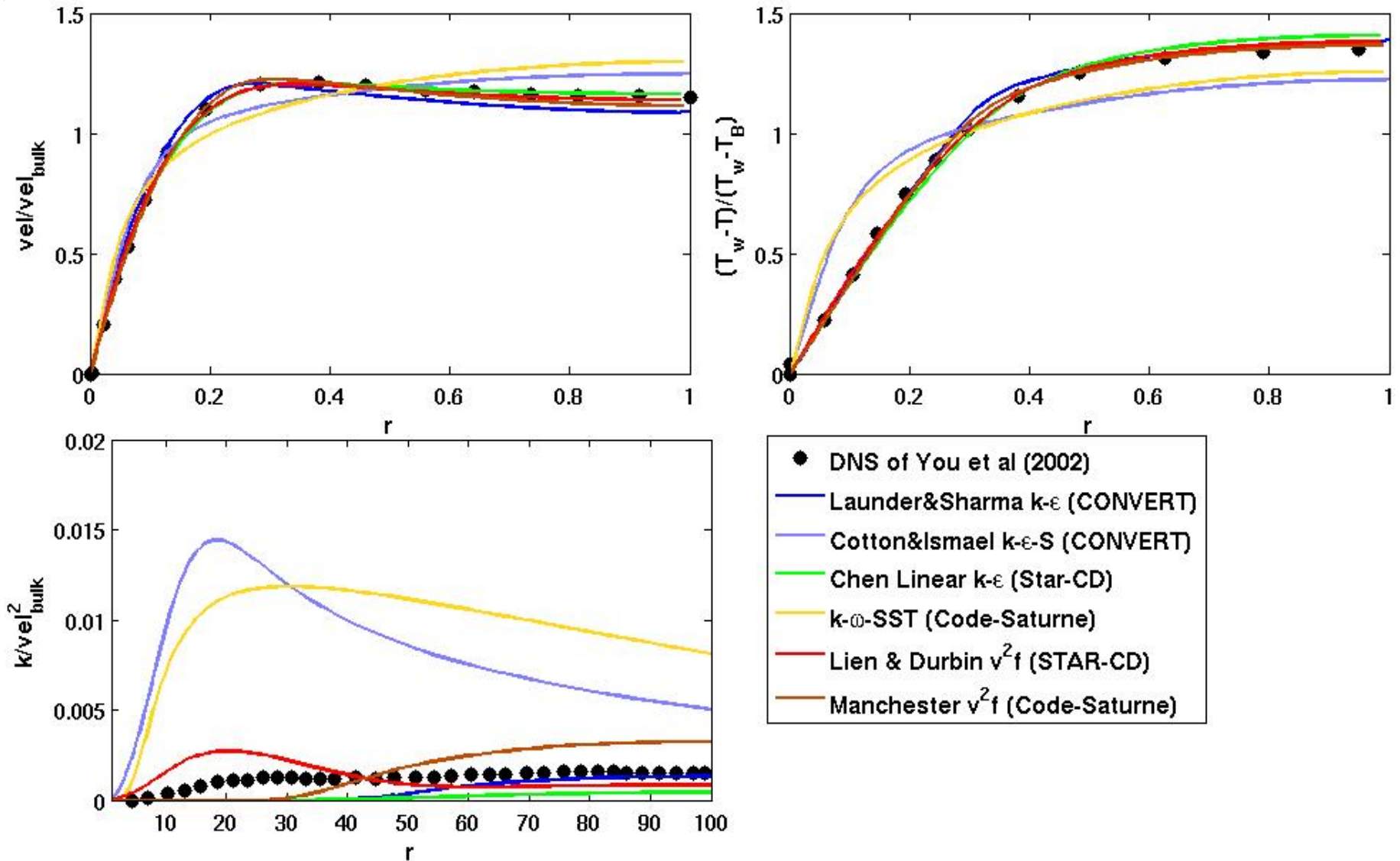


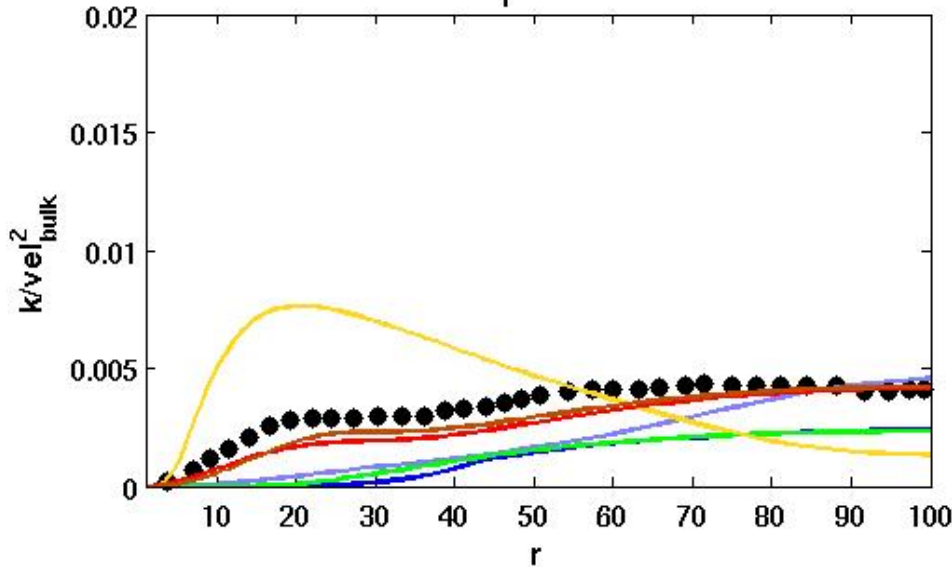
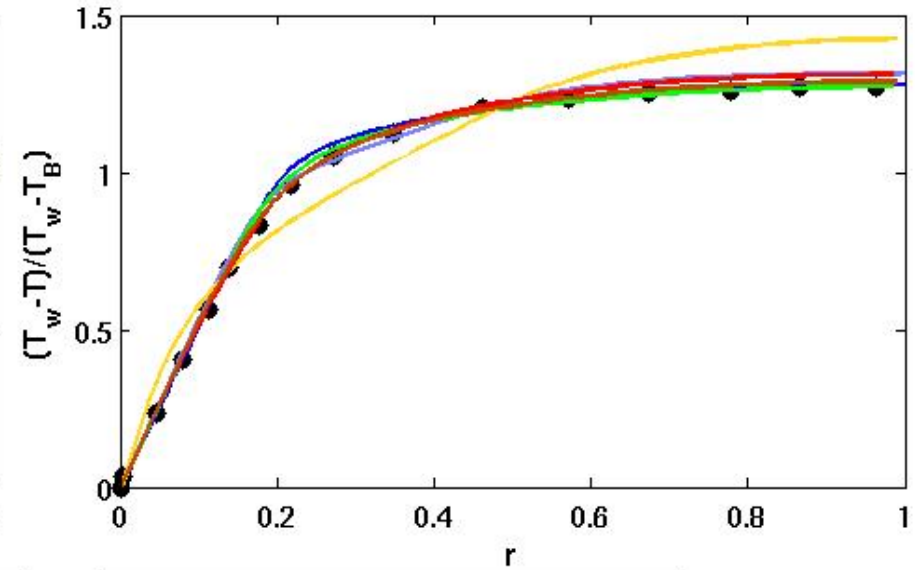
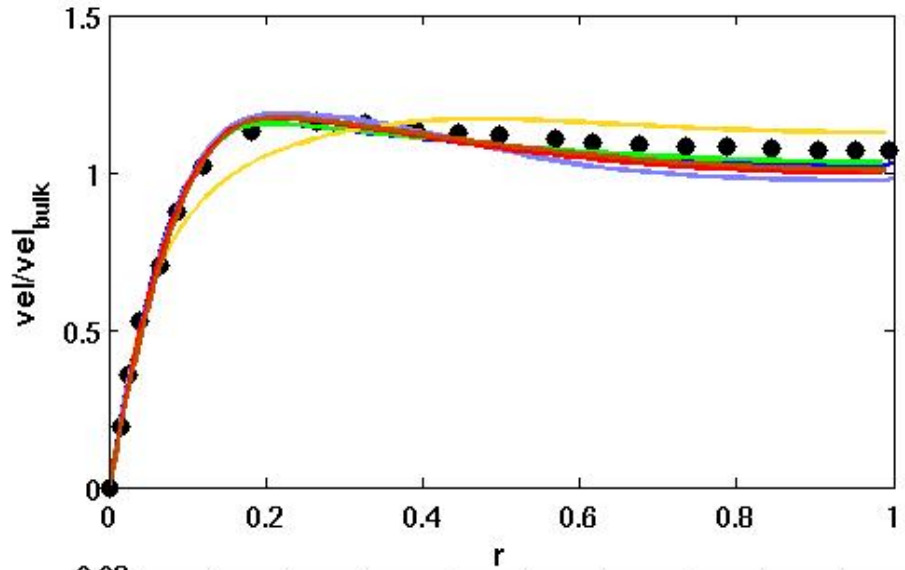
- DNS of You et al (2002)
- Launder&Sharma k-ε (CONVERT)
- Cotton&Ismael k-ε-S (CONVERT)
- Chen Linear k-ε (Star-CD)
- k-ω-SST (Code-Saturne)
- Lien & Durbin v^2f (STAR-CD)
- Manchester v^2f (Code-Saturne)

$$Gr/Re^{**2} = 0.063$$



$Gr/Re^{**2} = 0.087$ (relaminarization)



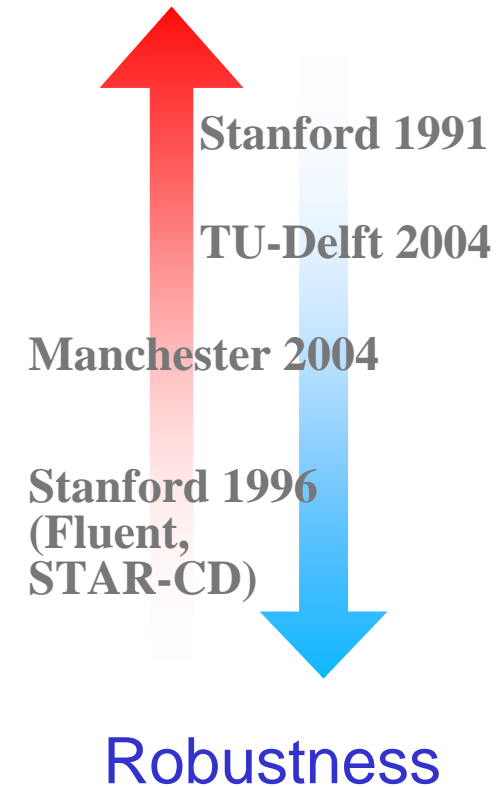


- DNS of You et al (2002)
- Launder&Sharma k-ε (CONVERT)
- Cotton&Ismael k-ε-S (CONVERT)
- Chen Linear k-ε (Star-CD)
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- Manchester v^2f (Code-Saturne)

The $\overline{v^2} - f$ model and *Code_Saturne*

- A low-Reynolds (near-wall integration) eddy viscosity model derived from second moment closure models
- No damping functions, no wall functions, less empirical assumptions
- Best results on range of test cases, heat transfer and natural convection in particular.
- The original model is stiff (requires coupled solver or very small time-step)
- Degraded version available in StarCD, Fluent, NUMECA..
- Long collaboration Stanford, Delft, Chatou, Manchester (Durbin, Parneix, Hanjalic, Manceau, Uribe)
=> “several code friendly” versions since 1995.
- Present: Reconsider all historical choices with numerical stability and known asymptotic states as principal objectives

Accuracy



Durbin's original model

Classic near wall model

$$\nu_t = f_\mu C_\mu k T \quad ; \quad T = k / \varepsilon$$

$$f_\mu = \frac{\nu_t \text{ you want}}{\nu_t \text{ you have}}$$

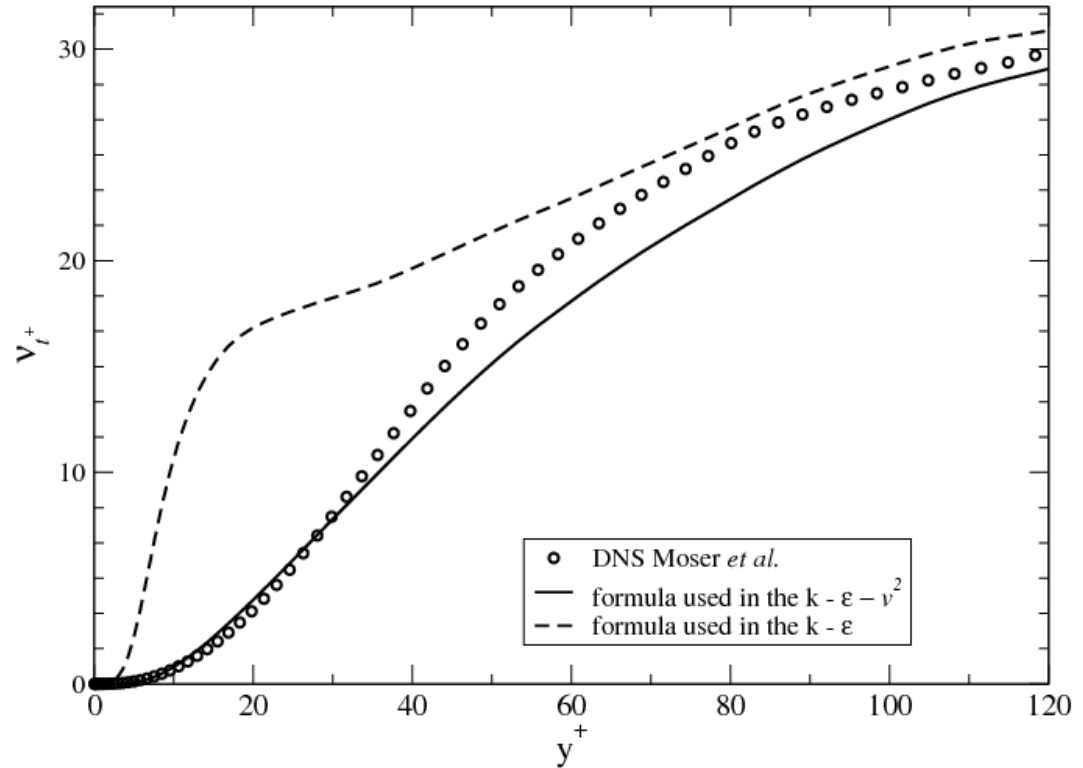
$$f_\mu = f(y^+, \nu_t / \nu)$$

Elliptic Relaxation

$$\nu_t = C_\mu \overline{\nu^2} T$$

$$\frac{D\overline{\nu^2}}{Dt} = \phi_{22} - \varepsilon_{22} + \nabla \cdot ((\nu + \nu_t) \nabla \overline{\nu^2})$$

$$\phi_{22} = -\frac{2}{\rho} \overline{\nu \partial p' / \partial y}$$



the walls affect the whole domain through an elliptic operator : near wall effects (mainly wall echo and wall blocking effect)

The usual second moment closure

- Usual closure for the source term of $\overline{v^2}$:

$$\frac{D\overline{v^2}}{Dt} = \overline{\phi_{22}} - \left(\varepsilon_{22} - \frac{2}{3} \varepsilon \right) - \frac{2}{3} \varepsilon + \text{Diff}_{v+v_t} \overline{v^2}$$

$\overline{\phi_{22}}$ Term to be modelled

Model for the dissipation : $\varepsilon_h = \frac{2}{3} \varepsilon$

Launder Reece Rodi (LRR) :

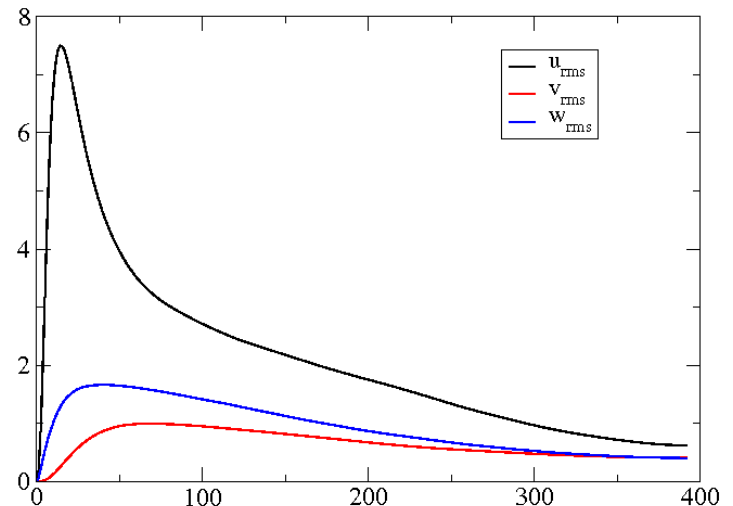
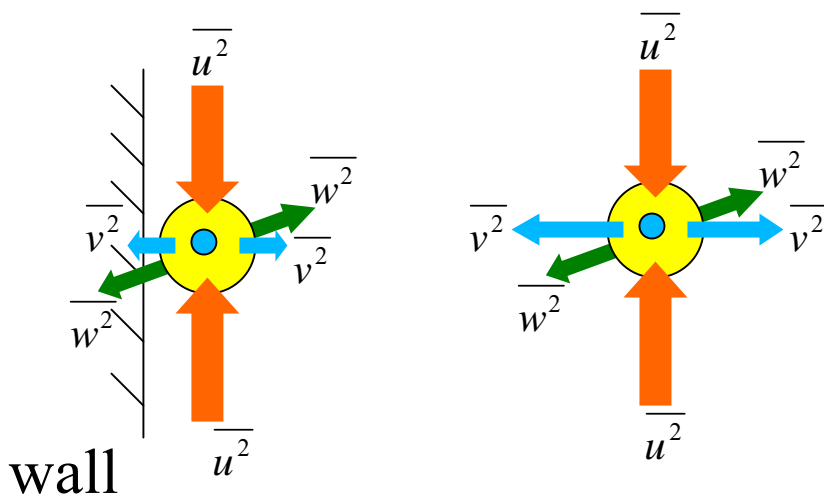
$$\phi_{22}^h = -\frac{1}{T} C_1 \left(\frac{\overline{v^2}}{k} - \frac{2}{3} \right) + C_2 \frac{P}{k}$$

Speziale, Sarkar, Gatski (SSG) :

$$\phi_{22}^h = -\frac{1}{T} \left(C_1 + C'_2 \frac{P}{\varepsilon} \right) \left(\frac{\overline{v^2}}{k} - \frac{2}{3} \right) - \left(\frac{C_4}{3} - C_5 \right) \frac{P}{k}$$

Wall blocking effect:

The redistribution is anisotropic near the wall




The asymptotic behaviour

- Near wall limit of the k - ϵ model $k = O(y^2)$ $\epsilon = O(1)$

$$\frac{Dk}{Dt} = \underbrace{(\nu + \nu_t) \Delta k}_{(O(1)+O(y^3)) \cdot \Delta O(y^2)} + \underbrace{P}_{O(y^3)} - \underbrace{\epsilon}_{O(1)} \approx \nu \Delta k - \epsilon \approx \nu \Delta k^{n+1} - \left(\frac{\epsilon}{k}\right)^n k^{n+1}$$

Negative
but implicit
source



No stability problem

The asymptotic behaviour

two-component limit of the turbulence

- Taylor series expansion : $\overline{u^2} = O(y^2)$ $\overline{w^2} = O(y^2)$ $\overline{v^2} = O(y^4)$

term to be modelled

$$\frac{D\overline{v^2}}{Dt} = \underbrace{v \frac{\partial^2 \overline{v^2}}{\partial x_k^2}}_{O(y^2)} - \underbrace{\frac{\partial \overline{v^2} u_i}{\partial x_i}}_{O(y^5)} + \underbrace{\overbrace{\phi_{22}}^{O(y)} + \overbrace{D_{22}^p}^{O(y)}}_{O(y^2)} - \underbrace{\left(\varepsilon_{22} - \frac{\varepsilon}{k} \overline{v^2} \right)}_{O(y^2)} - \underbrace{\frac{\varepsilon}{k} \overline{v^2}}_{O(y^2)}$$

Ay^2 $By^2 = k f$ Cy^2

The balance between quadratic terms must be ensured

$$A + B + C = 0 \quad \text{near the wall}$$

$$(+6) + (-5) + (-1) = 0$$

$$L^2 \nabla^2 f - f = f_{\text{hom}} \quad \text{with} \quad \lim_{y \rightarrow 0} f = -20 v^2 \lim_{y \rightarrow 0} \left(\frac{\overline{v^2}}{\varepsilon y^4} \right) \Rightarrow = -\frac{O(y^4)}{O(y^4)} !$$

Stanford “code friendly” model (1)

Lien and Durbin (1996)

- It involves a change of variable $f = \bar{f} + g$ so that $\lim_{y \rightarrow 0} \bar{f} = 0$

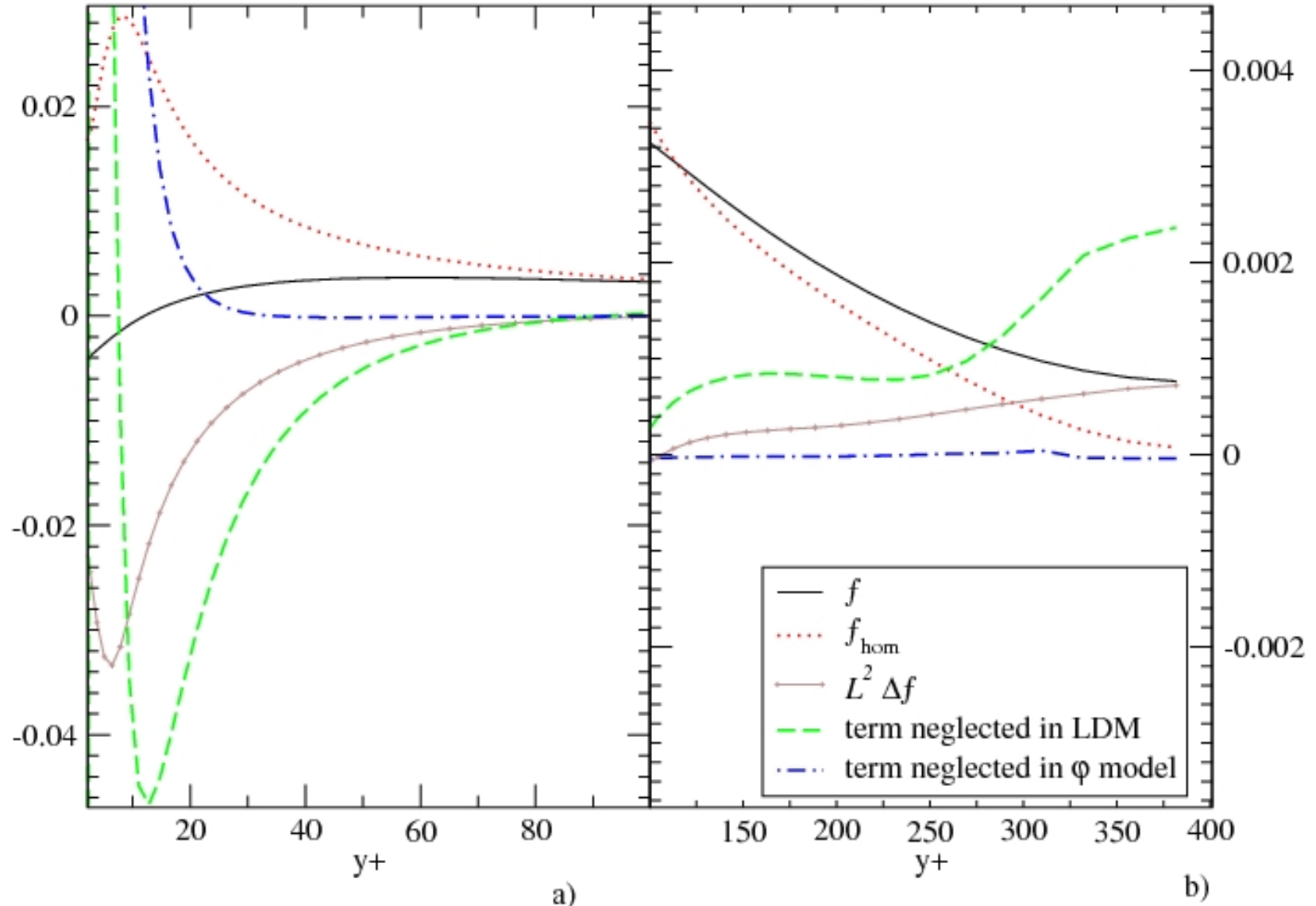
Original Durbin : $0 = Ay^2 + \underset{k f}{By^2} + Cy^2$

Stanford : $0 = Ay^2 + \underset{k f - k g}{By^2 - Dy^2} + Cy^2 + \underset{k g}{Dy^2}$
 $B - D = 0$

- The new equation for f reads :

$$L^2 \nabla^2 \bar{f} - \bar{f} = \frac{C_1 - 1}{T} \left(\frac{\bar{v}^2}{k} - \frac{2}{3} \right) - C_2 \frac{P}{\varepsilon} + g - \underbrace{L^2 \nabla^2 g}_{\text{neglected term}}$$

Stanford "code friendly" model (2)



Delft / UMIST approach

UMIST (Laurence *et al.* (2004)) and TU-Delft (Hanjalic *et al.* (2004))

- A new change of variable to reduce the stiffness of the B.C. : $\varphi = \frac{\overline{v^2}}{k} \rightarrow f_w = -2\varepsilon \frac{\varphi}{y^2}$

$$\frac{D\varphi}{Dt} = \underbrace{f}_A - P \frac{\varphi}{k} + \frac{2}{k} \left(\underbrace{\nu + \frac{\nu_t}{\sigma_k}}_B \right) \underbrace{\nabla\varphi \nabla k}_{C} + \nabla \left(\left(\underbrace{\nu + \frac{\nu_t}{\sigma_\varphi}}_C \right) \nabla \varphi \right)$$

$$A = -(B + C) \quad \text{near the wall}$$

UMIST φ model

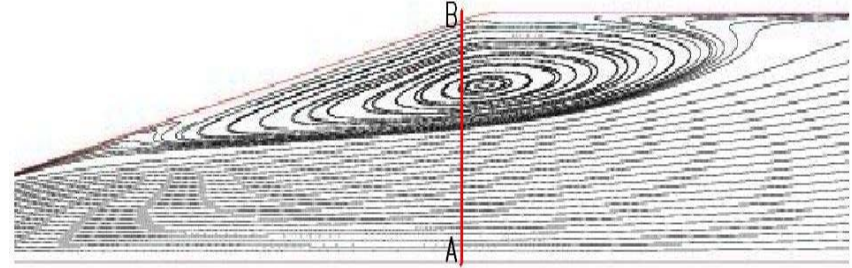
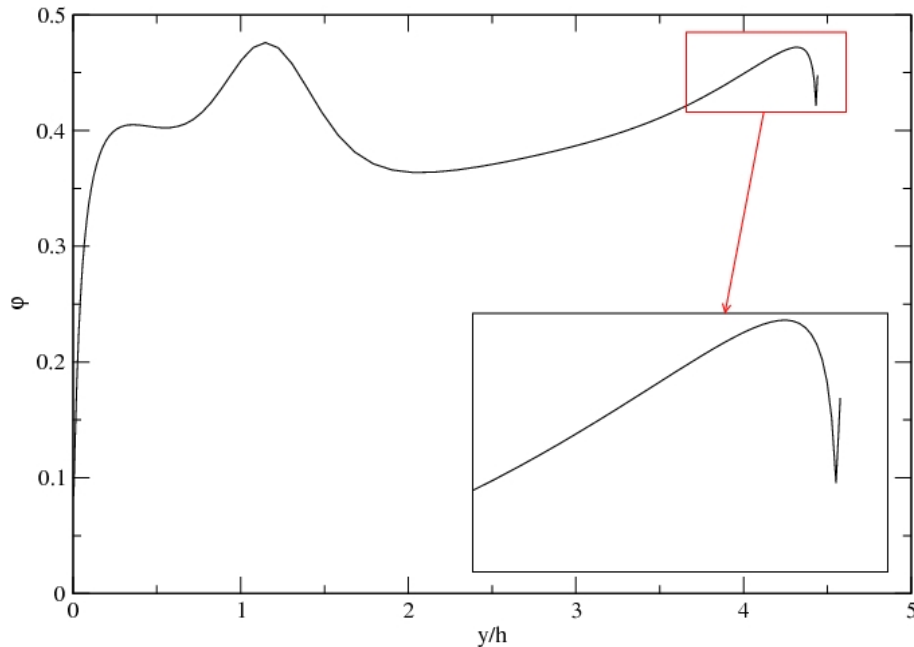
$$\overline{f} = f + \frac{2}{k} \nu \nabla\varphi \nabla k + \nu \nabla^2 \varphi$$

$$f_w = 0$$

Delft ζ model

$$f_w = -2\varepsilon \frac{\zeta}{y^2}$$

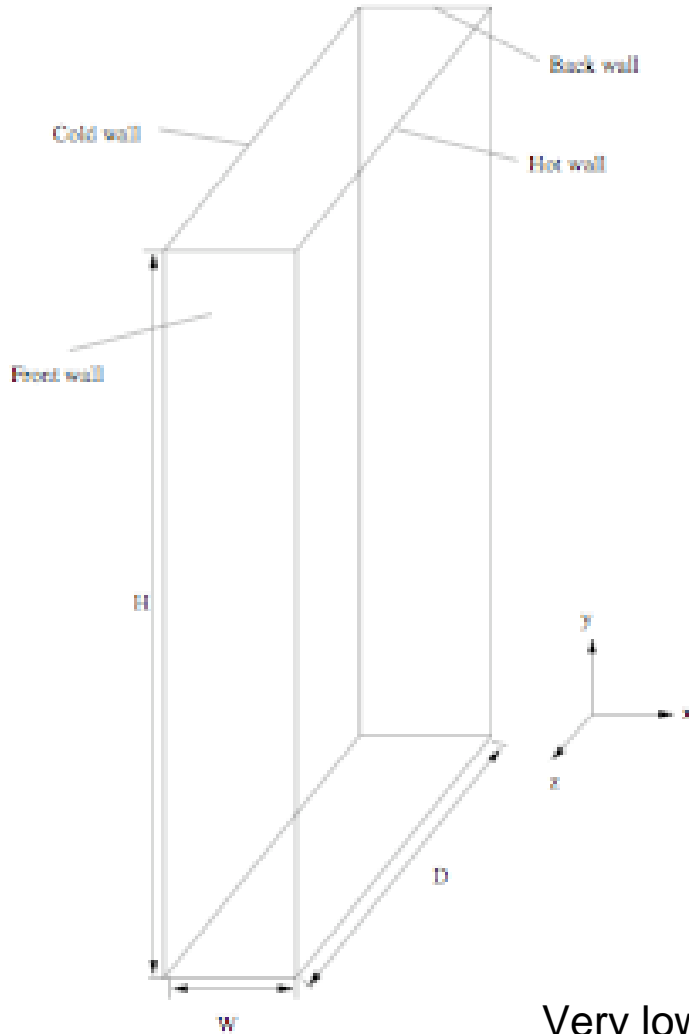
Numerical instabilities of the $\varphi = \frac{\overline{v^2}}{k}$ model



2 options :

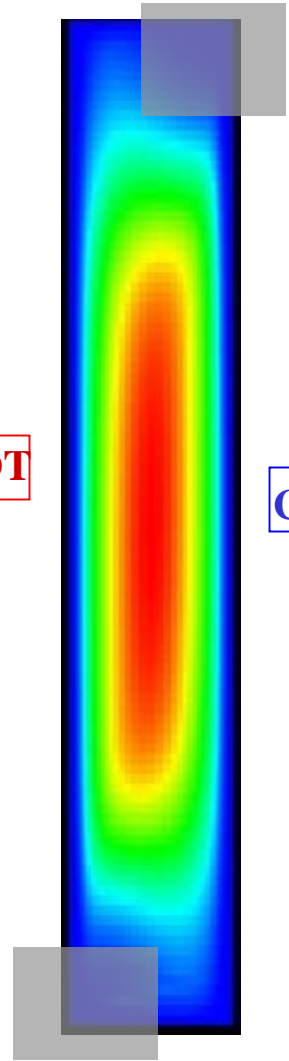
- f is forced to be equal to 0 at the wall : excellent robustness, similar to the one of Stanford's model, but bad prediction of the turbulent viscosity near the wall.
- the turbulent viscosity is removed : numerical instabilities

Natural convection in a heated cavity (non convergence in C_S V 1.2 !)



HOT

COLD



Very low value of k

Very low value of k

Code_Saturne

φ model

$$\bar{f} = f + \frac{2}{k} \nu \nabla \varphi \nabla k + \nu \nabla^2 \varphi$$

The $\varphi - \alpha$ model

- Using the elliptic blending of Manceau and Hanjalic 2002 (with Re stress model)

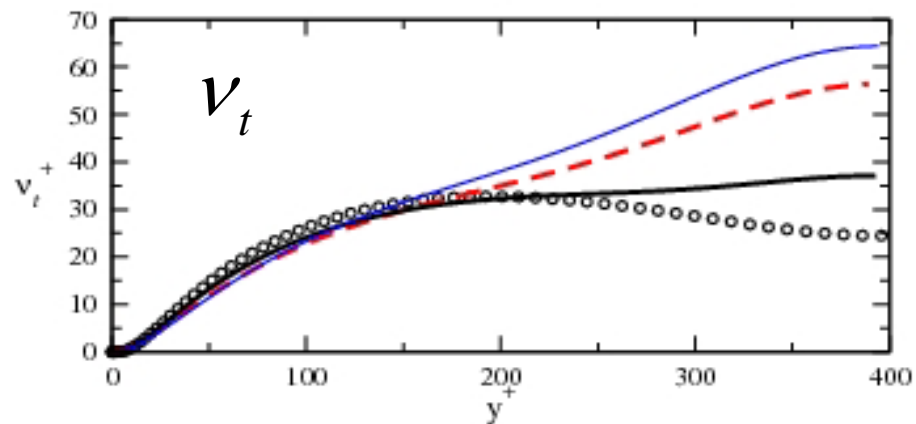
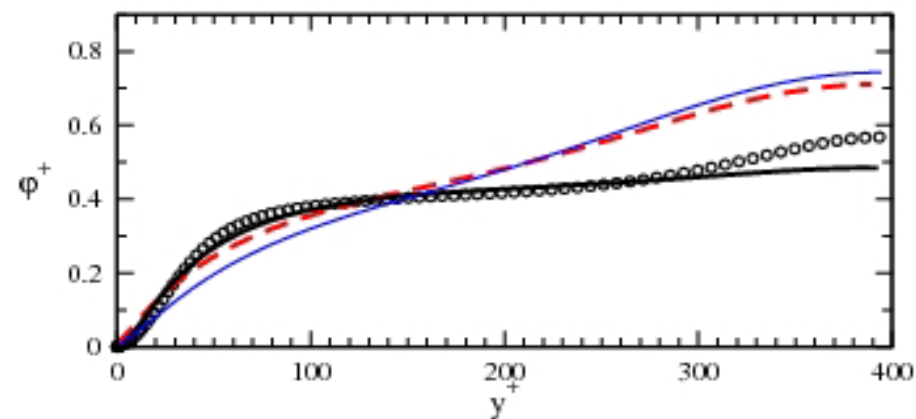
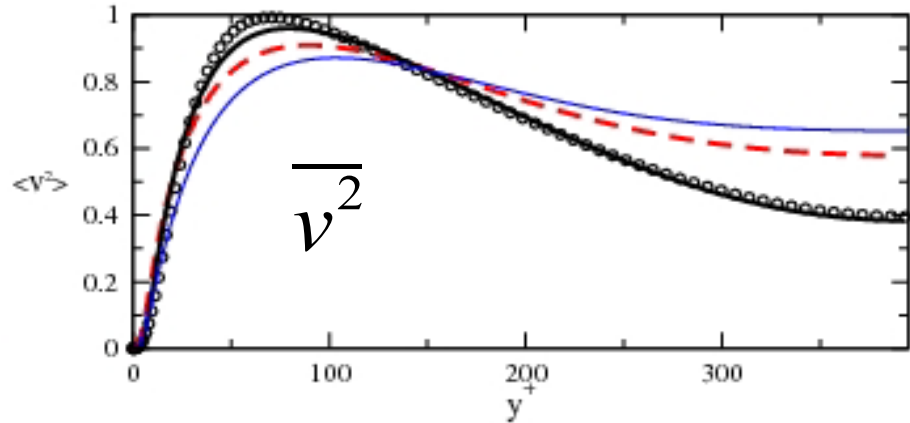
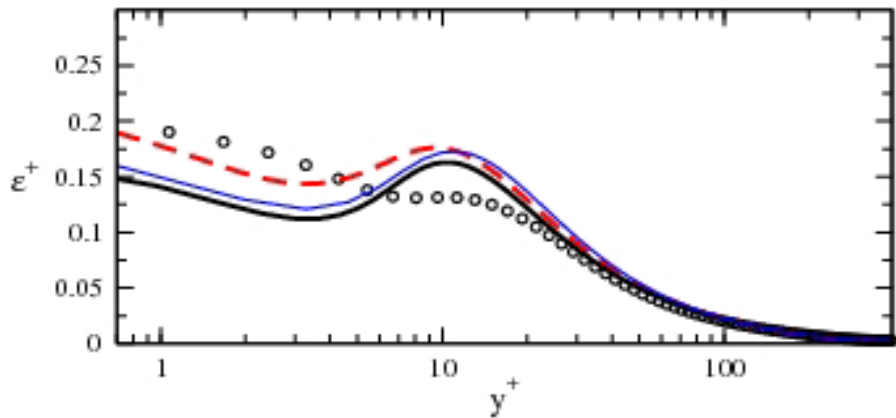
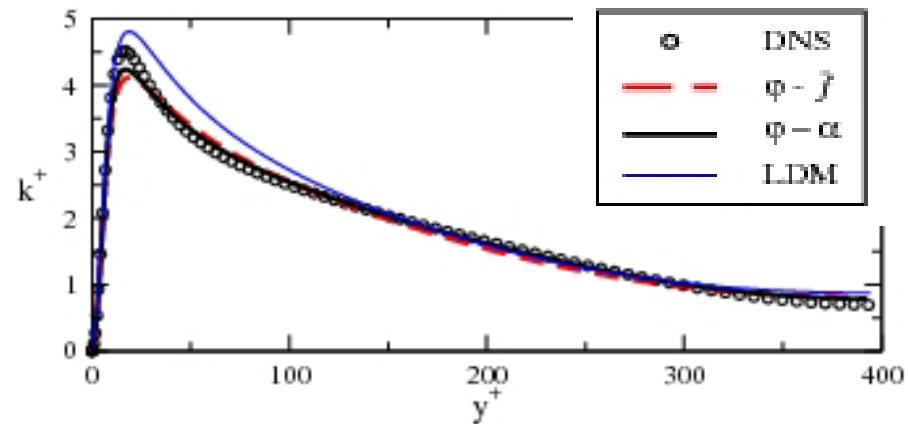
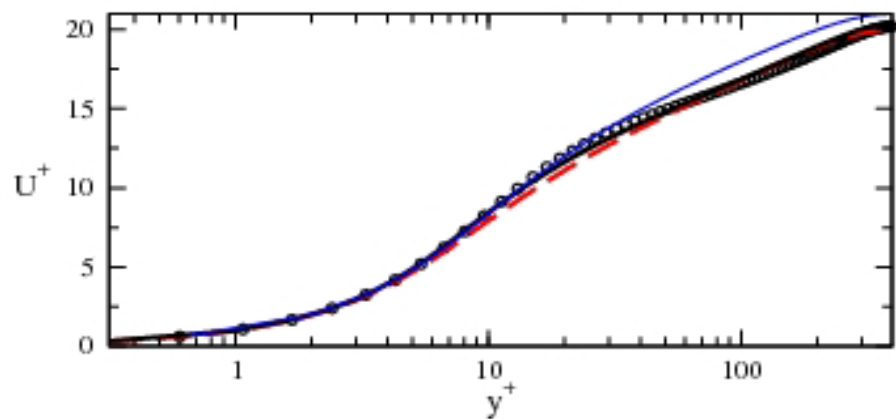
$$L^2 \nabla^2 \alpha - \alpha = -1 \quad \Bigg| \quad \alpha_w = 0$$

$$\frac{D\varphi}{Dt} = \alpha^3 f_{hom} + (1 - \alpha^3) f_w - P \frac{\varphi}{k} + \frac{2\nu_t}{k} \underline{\nabla} \varphi \underline{\nabla} k + \nabla \left(\left(\nu + \frac{\nu_t}{\sigma_\varphi} \right) \nabla \varphi \right)$$

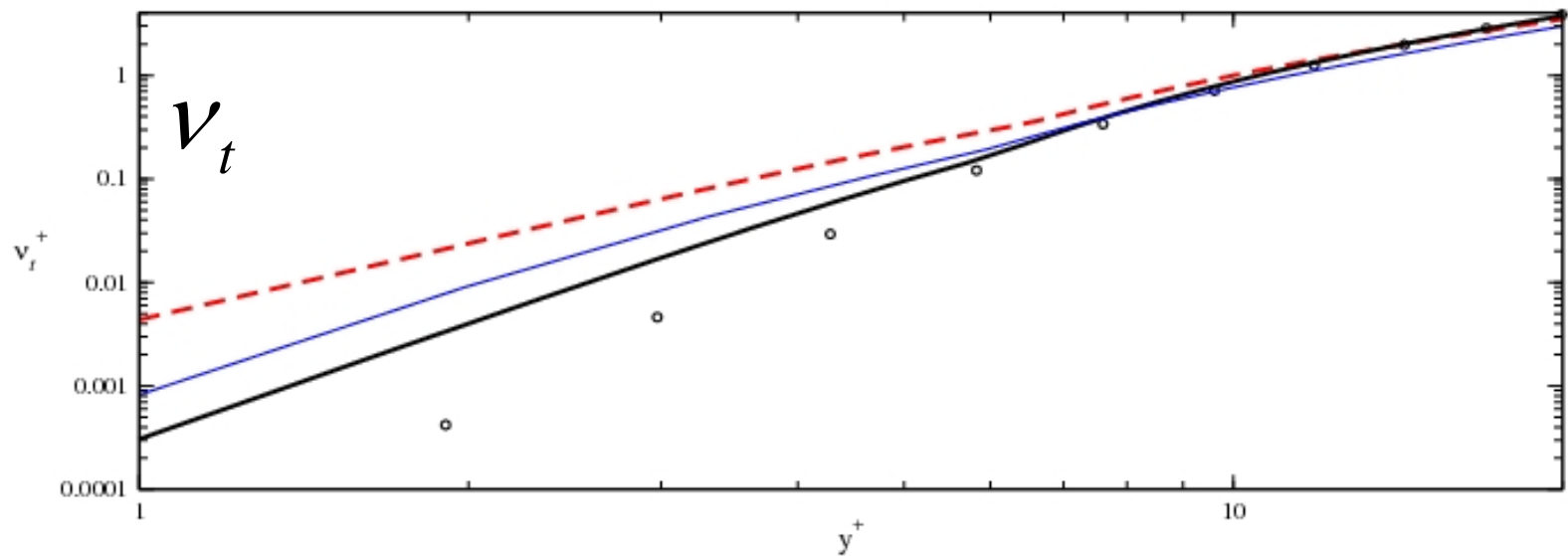
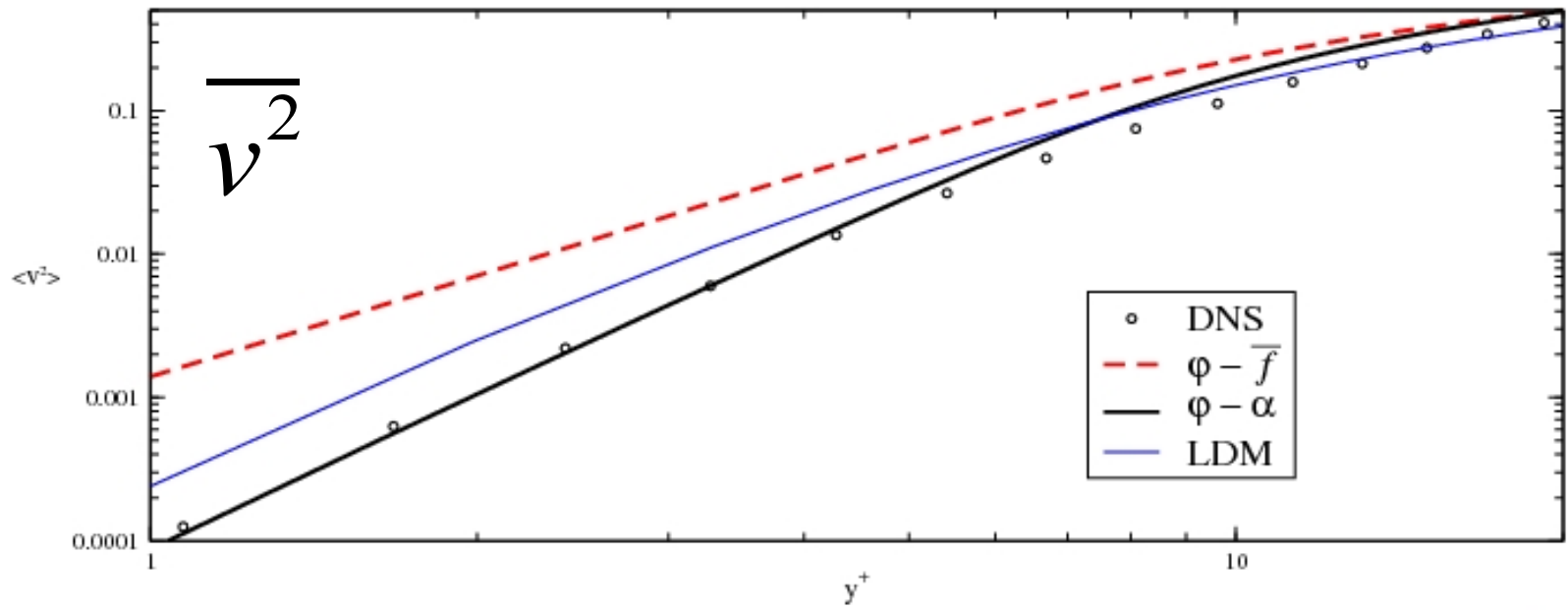
$$f_w = -\varepsilon \frac{\varphi}{y^2} \quad \longrightarrow \quad f_w - \nu \nabla^2 \varphi = o(1)$$

- Successfully tested on channel flows for many Re numbers, flow around airfoil trailing edge, heated pipe, heated channel flow, heated cavity
- Normal time-step (external flow CFL values as for k-omega)
- Unlike, code friendly Stanford model, no term has been neglected here
- Unlike UMIST and Delft model, the correct asymptotic behaviour of ν^2 and ν_t is accurately predicted without impairing the numerical robustness

Results (Channel flow, $Re^*=395$)



Results (Channel flow, $Re^*=395$) (2)



Conclusions and further work

- 4 different versions of V2F revisited => numerical stability improved while respecting known asymptotic states,
- Relaminarisation OK,
next: prediction of laminar-turbulent transition,
input some ingredients of Launder and Sharma model
(extra viscous source terms in epsilon equation)
- Recalibration of source terms in the ε equation
(all literature focuses only on near wall layer
but prediction of the core region can be improved)
- An accurate and robust near-wall low-Reynolds RANS model also suitable for RANS/LES coupling

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- [1] Launder, B.E. and Sharma, B.I., 1974, *“Application of the energy dissipation model of turbulence to the calculation of flow near a spinning disc”*, Lett. Heat Mass Transfer, 1, pp. 131-138.
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- [5] Durbin, P.A. 1995, *“Separated flow computations with the k - ϵ - v^2 model”*, AIAA Journal, 33(4), pp. 659–664.
- [6] Laurence, D., Uribe, J.C. and Utyuzhnikov, S., 2004, *“A robust formulation of the v^2 - f model”*, Flow, Turbulence and Combustion, 73, pp. 169-185
- [7] You, J., Yoo, J.Y. and Choi. H., 2003, *“Direct Numerical Simulation of Heated Vertical Air Flows in Fully Developed Turbulent Mixed Convection”*, Int. J. Heat Mass Transfer, 46, pp.1613-1627
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